

- Trans-Atlantic aircraft often fly at 37,000 ft. Are they flying in the troposphere or stratosphere?

$$1000 \text{ ft} = 0.305 \text{ km} \Rightarrow h = 37,000 \text{ ft} \left(0.305 \frac{\text{km}}{1000 \text{ ft}} \right)$$

$$h = 11.3 \text{ km} \quad \text{Stratosphere.}$$

- What is the outside air temperature at 37,000 ft?

From Fig 1.8, $T_{11 \text{ km}} \sim 217 \text{ K} = -56^\circ \text{C}$

4. The average tropopause height is 17 km in the tropics.

- Using the hydrostatic equation, what is the approximate pressure at the tropical tropopause?

$$p = 1000 \exp(-17/7) = 88 \text{ hPa}$$

- How far below the tropopause do trans-oceanic flights fly in the tropics?

$$17 - 11 = 6 \text{ km}$$

- What is the typical air temperature at the tropical tropopause?

from Figure 1.10, about 200 K (-70°C)

5. Assume an average global tropopause of 14 km and that the temperature is constant with altitude (i.e., use a constant scale height of 7 km.). Obtain a mathematical expression for the fraction of air density that is in the troposphere. What is the actual numerical fraction?

Consider the column density only. Column density $\equiv D = \int_0^z \rho(z) dz$

$$D = \int_0^z \rho_0 \exp(-z/H) dz = -H \rho_0 \exp(-z/H) \Big|_0^z = H \rho_0 (1 - \exp(-z/H))$$

For the whole column, $z = \infty$; for the trop $z = z_t \sim 14 \text{ km}$

$$\therefore \text{fraction} = H \rho_0 (1 - \exp(-z_t/H)) / H \rho_0 = 1 - \exp(-z_t/H) = 1 - \exp(-14/7) = 86\%$$

6. In class, we found that the atmospheric mass is approximately $5 \times 10^{18} \text{ kg}$.

- What is the approximate number of moles in the atmosphere?

Mass per mole = 0.029 kg/mole $\therefore \# \text{ moles} = \frac{5 \times 10^{18} \text{ kg}}{0.029 \text{ kg/mole}} = 1.7 \times 10^{20} \text{ moles}$

- What is the approximate number of molecules in the atmosphere?

By Avagadro's number, each mole has 6.02×10^{23} molecules

$$\# \text{ molecules} = 1.7 \times 10^{20} \times 6.02 \times 10^{23} \approx 10^{44} \text{ molecules.}$$