

7. From your physics courses, you know that a molecule's thermal energy is given by  $E = (3/2)kT$ , where  $k$  is the Boltzmann constant and  $T$  is the temperature in Kelvin.

- What is the energy in a mole of gas at 273 K?

$$R^* = k N_{\text{Avogadro}} = 8.3 \text{ J deg}^{-1} \text{ mole}^{-1} \quad E = \frac{3}{2}(8.3)(273) = 3.4 \times 10^3 \text{ J/mole}$$

- How many moles of gas are in a  $\text{m}^3$  of space if  $T = 273 \text{ K}$  and  $p = 1013 \text{ hPa}$ ?

$$\rho_{\text{STP}} \approx 1.28 \text{ kg m}^{-3}. \text{ Each mole has a mass of } 0.029 \text{ kg/mole}$$

$$\# \text{ moles} = (1.28 \text{ kg m}^{-3}) / (0.029 \text{ kg/mole}) = 44.6 \text{ moles m}^{-3}$$

- What is the thermal energy of a  $\text{m}^3$  of air at STP ( $T = 273 \text{ K}$  and  $p = 1013 \text{ hPa}$ )?

$$E = 44.6 \frac{\text{mole}}{\text{m}^3} \cdot 3.4 \times 10^3 \frac{\text{J}}{\text{mole}} = 1.5 \times 10^5 \text{ J} \quad \left( \begin{array}{l} 1 \text{ Watt} = 1 \text{ J/s} \dots 1.5 \times 10^5 \text{ J} \\ \text{runs a computer for 8 min.} \end{array} \right)$$

- Assuming an average temperature for the atmosphere of 250 K, what is the thermal energy in the atmosphere?

$$\text{Atmosphere has } 1.7 \times 10^{20} \text{ moles. } E_{\text{atm}} = (1.7 \times 10^{20}) \frac{3}{2} (8.3)(250) = 5.3 \times 10^{23} \text{ J}$$

- A stiff wind at Earth's surface is  $30 \text{ m s}^{-1}$ . What is the energy associated with one  $\text{m}^3$  of air that is traveling at this speed?

$$E = \frac{1}{2} m v^2 = \frac{1}{2} \rho V v^2 = \frac{1}{2} (1.28 \text{ kg m}^{-3})(1 \text{ m}^3)(30 \text{ m s}^{-1})^2 = 580 \text{ J}$$

- How does this compare to your answer for the amount of thermal energy in  $1 \text{ m}^3$  of air?

$$\text{It is } (1.5 \times 10^5) / (580) = 130 \text{ times less.}$$

8. Consider a small fair-weather cumulus cloud (like those you see on a nice summer's day). If the liquid water content (LWC) is  $0.3 \text{ g m}^{-3}$ , what is the total liquid water mass in the cloud? State your estimate of the cloud's size.

A good size fair weather cumulus cloud is about equivalent to a 100 m radius sphere.

$$\text{Total liquid water} = \frac{4}{3} \pi (r)^3 \cdot \text{LWC} = \frac{4}{3} \pi (100)^3 \cdot 0.3 = 1.2 \times 10^3 \text{ kg} \\ \sim 1.2 \text{ ton}$$

9. Satellites often fly a few hundred kilometers above Earth's surface. Why don't they burn up during an active sun period?

During an active sun,  $T \sim 2000 \text{ K}$ ! But what is the total energy encountered during 1 orbit?

$$E = \frac{3}{2} (\# \text{ molecules}) k T = \frac{3}{2} \left( \underset{\substack{\uparrow \\ \text{from Fig 1.5}}}{10^{15} \frac{\text{molecules}}{\text{m}^3}}} \cdot \underset{\substack{\uparrow \\ \text{satellite size}}}{1 \text{ m}^2} \cdot 2\pi \underset{\substack{\uparrow \\ \text{orbit path}}}{(6.8 \times 10^6 \text{ m})} \right) \times$$

$1.4 \times 10^{-23} \text{ J deg}^{-1} \text{ molecule}^{-1} \cdot 2000 \approx 2000 \text{ J}$ . An orbit takes about 1 hour, so the Watts of heating is .5 W from this effect.