

Meteo 431 Atmospheric Thermodynamics Spring 2002

Problem set # 9

assigned: 17 April 2002

due: 24 April 2002

1. B&A, Chapter 6, #3.
2. B&A, Chapter 6, #5. (hint: What temperature is the lowest temperature that air can be cooled by evaporation? Use the skew-T.)
3. B&A, Chapter 6, #6.
4. B&A, Chapter 6, #8.
5. B&A, Chapter 6, #22
6. B&A, Chapter 6, #24.

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① B&A, #3 For 400% RH to have clouds form,

$$e_s^{\text{new}}(T_n) = 4 e_s(T_d) \Rightarrow \exp\left(-\frac{L_v}{R_v T_n}\right) = 4 \exp\left(-\frac{L_v}{R_v T_d}\right)$$

$$-\frac{L_v}{R_v T_n} = \ln 4 - \frac{L_v}{R_v T_d} \Rightarrow -\frac{L_v}{R_v} T_d = T_n T_d \ln 4 - \frac{L_v}{R_v} T_n$$

$$T_n = \frac{\frac{L_v}{(L_v - \ln 4 R_v T_d)} \cdot T_d}{\frac{2.5 \times 10^4}{2.5 \times 10^4 - 639 T_d} \cdot T_d}$$

$$\Delta T = T_n - T_d = \frac{639 T_d^2}{2.5 \times 10^4 - 639 T_d}$$

for $T_d = 290 \text{ K}$, $\Delta T = 23 \text{ K}$

for $T_d = 300 \text{ K}$, $\Delta T = 25 \text{ K}$

$T_d = 270 \text{ K}$, $\Delta T = 20 \text{ K}$

} since T_d is unchanged,
and T must now drop
 $\sim 20-25 \text{ K}$ more, the
LCL increases by
2 to 2.5 km.

We can do this on a skew-T by choosing a w_s that
is 4 times greater than normal. If we assume $T = 10^\circ\text{C}$
② 1000 hPa, then $w_s = 1.5 \text{ g/kg}$ implies we need a
new $w_{sn} = 30 \text{ g/kg}$. ($T = 29^\circ\text{C}$)

If $T_d = 273 \text{ K}$, then old LCL = 860 hPa (1.4 km)

now, take $T = 29^\circ\text{C}$, and $T_d = 0^\circ\text{C}$ @ 1000 hPa

to get new LCL = 630 hPa (3.7 km)

$\Delta h \sim 2.3 \text{ km}$, in line with the other estimate.

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(2) B&A, Ch 6, #5. Assume very dry means RH = 10%

$$\text{If } T = 40^\circ\text{C}, w_s = \frac{e_s}{p - e_s} \quad e_s = 6.11 \exp \left\{ 6800 \left(\frac{1}{273} - \frac{1}{T} \right) - 5.09 \ln \left(\frac{313}{273} \right) \right\}$$

$$e_s = 73.8 \text{ hPa} \Rightarrow w_s = 50. \text{ g/kg} \Rightarrow w = 5 \text{ g/kg}$$

The lowest temperature to which air can be cooled by evaporation is the wetbulb T.

- Find LCL & Take moist adiabat down from there to $p = 1000 \text{ hPa}$ (assume for Arizona)

$$T_{wb} = 18^\circ\text{C} \quad (64^\circ\text{F})$$

(3) B&A, ch 6, #6 $T_d = 75^\circ\text{F} = 23.9^\circ\text{C}$

$$T = 95^\circ\text{F} = 35^\circ\text{C}$$

Using the same procedure as for (2), $T_{wb} = 27^\circ\text{C} \quad (80^\circ\text{F})$

The dewpoint makes a huge difference.

(4) B&A, ch 6, #8 $\Theta_v = \left(\frac{p}{p} \right)^{\frac{R-1}{R}} (T + 0.608q)$

$$\Theta_v = \Theta + \left(\frac{p}{p} \right)^{\frac{R-1}{R}} 0.608q.$$

For a fixed p, take the derivatives with respect to z.

$$\frac{d\Theta_v}{dz} = \frac{d\Theta}{dz} + 0.608 \left(\frac{p_0}{p} \right)^{\frac{R-1}{R}} \frac{dq}{dz}. \quad \text{If } \frac{dq}{dz} < 0, \text{ then}$$

$$\frac{d\Theta_v}{dz} < \frac{d\Theta}{dz}. \quad \text{But } \frac{d\Theta}{dz} \text{ gives real stability. So}$$

$\frac{d\Theta}{dz}$ predicts a more stable atmosphere than exists.

⑤ B&A, Ch 6, #22. $p_0 = 850 \text{ hPa}$, $T = 10^\circ\text{C}$ $\text{RH} = 100\%$

a. Since $\text{RH} = 100\%$, go up the moist adiabat to 600 hPa.

$w_i = 9 \text{ g/kg}$. At 600 hPa, $w_s = 4.2$, so that

$w_w = 9 - 4.2 = 4.8 \text{ g/kg}$. Assume this is removed.

b. If all liquid is removed, $p = 600 \text{ hPa}$ is the new LCL.

Go down constant $w \neq \theta$ to 850 hPa. Now

$T = 23^\circ\text{C}$ and $\text{RH} = \frac{4.2}{20} = 21\%$ warm & dry.

⑥ B&A, Ch 6, #24.

In a cloud, the relative humidity is 100% and liquid water exists. Below the cloud, the relative humidity can be below 100%. Rain falling out of the cloud into the lower RH air starts to evaporate, but can hit the ground before all or much of it has evaporated.